

- buyer gets p^m units of money, which provides utility:

$$p^m \frac{\partial u}{\partial m} = \left(\frac{p^m}{p}\right) \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left(\frac{N}{p}\right)^{-1/\varepsilon}$$

- Seller enjoys surplus from trade:

$$S = \left(\frac{p^m}{p}\right) \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left(\frac{N}{p}\right)^{-1/\varepsilon}$$

All prices are the same, given by price man, so $p^m = p$.

$$S = \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left(\frac{N}{p}\right)^{-1/\varepsilon}$$

$$S > 0$$

- Buyer enjoys surplus from trade:

$$B = \frac{X}{1+x} \frac{\varepsilon-1}{\varepsilon} c^{-1/\varepsilon} - \left(\frac{p^m}{p}\right) \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left(\frac{N}{p}\right)^{-1/\varepsilon}$$

$$B = \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left[X c^{-1/\varepsilon} - \left(\frac{p^m}{p}\right) \left(\frac{N}{p}\right)^{-1/\varepsilon} \right]$$

$$B = \frac{1}{1+x} \frac{\varepsilon-1}{\varepsilon} \cdot \left[X c^{-1/\varepsilon} - \left(\frac{N}{p}\right)^{-1/\varepsilon} \right] \quad (\text{all prices are same})$$

FOC from household's problem: (used to compute AD curve)

$$X c^{-1/\varepsilon} = [1 + \tau(x)] \left(\frac{N}{p}\right)^{-1/\varepsilon}$$

$$B = \frac{1}{1+\chi} \cdot \frac{\varepsilon-1}{\varepsilon} \cdot \left[(1+\tau(\alpha)) (\nu/p)^{-1/\varepsilon} - (\nu/p)^{-1/\varepsilon} \right]$$

$$B = \frac{1}{1+\chi} \cdot \frac{\varepsilon-1}{\varepsilon} \cdot \tau(\alpha) \cdot (\nu/p)^{-1/\varepsilon}$$

$$B > 0$$

Conclusion:

- seller surplus: $S > 0$
- buyer surplus: $B > 0$
- total surplus from matches:

$$T = S + B > 0$$